

Multivariate Statistical Analysis Decision-making Hybrid Method for Road Traffic Safety Evaluation in Iran

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Abstract Obviously, improving the road safety and the efficient allocation of limited resources to the provinces according to their ranking should be done. This paper presents a hybrid method of multivariate statistical analysis-decision making to evaluate Iran road traffic safety. In order to solve the problems of road traffic safety, a macroscopic evaluation and traffic safety level classification in Iran was carried out. An index system which consists of 14 relative indexes for road traffic safety evaluation was established. The principal component analysis method was used to reduce the dimensions of the multi-index data. Based on this, 2 components were extracted. The Index of Road Traffic Safety (IRTS) was calculated to rank the provinces of the country. A K-means method was applied to classify the provinces. A TOPSIS technique was used to examine the status of each cluster in terms of safety levels. Results showed that there are 4 safety levels entitled good, average, weak and very weak. The levels are approximately similar to result of the rankings.

Keywords: principal component analysis, K-means, TOPSIS , Index of Road Traffic Safety.

1 Introduction

Road traffic accidents are one of the most prominent public health threats in the world [1]. According to statistics, each year, 1.2 million people die and 50 million people are injured in road accidents around the world [2]. Iran has one of the highest rates of traffic accident fatalities and injuries. Thus, road safety is one of the main concerns of the Iranian transportation industry and a great deal of expenditure is incurred to control road traffic accidents. This article attempts to recognize and rank the country's provinces that provides good information for transportation planners in terms of the following criteria: death rate of per 100,000 people, injury rate of per 100,000 people, death rate of per 100 kilometers, injury rate of per 100 kilometers, lighting rate per 100 kilometers, speed camera rate of per 100

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kilometers, death rate to daily traffic volume, injury rate to daily traffic volume, emergency bases rate of per 100,000 people, crescent bases rate of per 100,000 people, emergency bases rate of per 100 kilometers, crescent bases rate of per 100 kilometers, average hours of driver training and the number of active police stations. Obviously, improving road safety and the efficient allocation of limited resources to the provinces according to their ranking is done. For this purpose, an indexing system which consists of 14 relative indexes for the road traffic safety evaluation was established. The principal component analysis method was used to reduce the dimensions of the multi-index data. The Index of Road Traffic Safety (IRTS) was produced in order to rank the road traffic safety situation. The K-means clustering method was applied to classify provinces taking two principal components. Finally, multi-criteria decision-making techniques such as TOPSIS were implemented in order to examine the status of each cluster in terms of safety levels. One of the main advantages of this paper is the combination of multi-criteria decision-making and multivariate statistical analysis techniques in the ranking of provinces.

The current paper is outlined as this. Section 2 contains a review of the previous studies conducted on ranking. In Section 3, the methodology and introduction to the principal component analysis (PCA)-cluster analysis(CA) method and the TOPSIS technique are discussed. In Section 4, the data used is described. Analysis of the results is given in section 5. Finally, the conclusion to our study is presented in Section 6.

2 Literature review

Fancello et al. [3], who examined road networks of suburban Sardinia, Italy, using a decision support system based on Electre III. This means that the main route is divided into 10 homogeneous segments to assess the safety with indicators such as peak hours, the percentage of heavy vehicles and accident rate. Khorasani et al. [4], evaluated the safety performance of 21 European countries. These are analyzed using decision-making methods such as SAW, AHP and Fuzzy TOPSIS. For this purpose, 11 indicators including the following were defined: the rate of the use of seat belts for front and rear seats, the percentage of cars with an average age of over 6 years, the cost of health care as a share of GDP, the average age of the passenger fleet, the share of motorcycles in the fleet, the volume of heavy vehicles in the fleet and the share of motorcycles in total road network.

Lin et al. [5], who examined China's road traffic safety in macroscopic indexes which consisted of 14 relative indexes. These indexes were established having taken into account the human, vehicle, road, and socio-economic synthetic influences by principal component analysis-cluster analysis method. Ahmadvand et al. [6], evaluated the performance of their selected provinces' road safety by applying model of data envelopment analysis (DEA) with principal component analysis. These focused on input variables such as age of the fleet, the percentage of roads with lighting, the percentage of highways, the elimination of black spots, the number of police stations in each province and the percentage of train users.

Furthermore, the output variables in the number of accidents and deaths were also investigated. The road safety situation of the Bushehr province is investigated by Haghigat [7]. In this study, all measures affecting road safety standards of the Bushehr province were categorized using the group analytic hierarchy process (GAHP). Following this, the roads of the Bushehr province were ranked using TOPSIS. Wei and Sun [8], who investigated the road safety of the eastern provinces of China with on the basis of improved principal component analysis and cluster analysis. Molla et al. [9], identified the principal components and factors

associated with road traffic crashes in the U.S. through a retrospective review based on more than two million records of fatal crashes over the space of 38 years (1975-2012). This information was taken from the National Highway Traffic Safety Administration Official's Fatal Accident Reporting System (FARS) database.

3 Methodology

In this section, we briefly explain the principal component analysis method that was used to reduce the dimensions of the multi-index. The K-means Clustering Analysis and TOPSIS methods that followed were described.

3.1 Principal component analysis

Principal component analysis (PCA) method was used to reduce dimensions of the multi-index data and extract principal components, and then, the Index of Road Traffic Safety (IRTS) was constructed for road traffic safety situation.

Suppose that X_{ij} is the value of the No. j index of No. i sample ($i=1,2,3,\dots,n$; $j=1,2,3,\dots,p$; n is the number of samples; P is the number of indexes), the steps of the PCA method are shown as follows[10]:

Step 1: Standardization of original index data In order to eliminate the influence of the order of magnitude and the dimensional effect on evaluation results, standardize the original index data according to Equation

$$X_{ij} = (x_{ij} - \bar{x}_j) / s_j \quad (1)$$

Where:

\bar{x}_j = Mean of the No. j sample index.

s_j = Standard deviation of the No. j sample index.

Step 2: Calculation index correlation matrix.

$$R = (r_{jk})_{p \times p} \quad j=1,2,3,\dots,p \quad ; \quad k=1,2,3,\dots,p \quad (2)$$

Where:

r_{jk} = The correlation coefficient of the No. j and the No. k indexes, can be computed as follows

$$r_{jk} = \frac{1}{n-1} \sum_{i=1}^n (Z_{ij} Z_{ik}) \quad \text{and} \quad r_{ii} = 1, r_{jk} = r_{kj} \quad (3)$$

Step 3: Calculation eigenvalues and eigenvectors

Solve the eigen equation $|\lambda_p - R| = 0$ to obtain the eigenvalues λ_g ($g=1,2,\dots,p$), then, arrange λ_g

in order of size: $\lambda_1 \geq \lambda_2 \dots \geq \lambda_p \geq 0$, the corresponding eigenvectors are $L_g = (L_{g1}, L_{g2}, \dots, L_{gp})$

Step 4: Calculate distribution rate and ascertain the number of principal components

Distribution rate of principal components is defined as:

$$\lambda_g / \sum_{g=1}^p \lambda_g \quad (4)$$

Cumulative distribution rate of the previous principal components is:

$$\sum_{i=1}^k \lambda_i / \sum_{g=1}^p \lambda_g \quad (5)$$

Step 5: Construction Index of Road Traffic Safety (IRTS)

$$IRTS = \sum_{g=1}^k \left[\left[\lambda_g / \sum_{g=1}^p \lambda_g \right] F_g \right] \quad (6)$$

Where:

F_g = The score of the No. g principal component can be calculated as follows[10]:

$$F_g = l_{g1}Z_1 + l_{g2}Z_2 + \dots + l_{gp}Z_p \quad (g = 1, 2, \dots, k) \quad (7)$$

The K-means clustering method was applied to safety level classification taking IRTS as variables.

3.2 K-means

The K-means algorithm is the simplest and most commonly algorithmis based on the square-error criterion. The general objective is to obtain the partition that, for a fixed number of clusters, minimizes the total square-error.

It starts with a random, initial partition and keeps reassigning the samples to clusters, based on the similarity between samples and clusters, until a convergence criterion is met. Typically, this criterion is met when there is no reassignment of any sample from one cluster to another that will cause a decrease of the total squared error [10].

Suppose that the given set of N samples in an n -dimensional space has somehow been partitioned into K clusters $\{C_1, C_2, \dots, C_K\}$. Each C_k has n_k samples and each sample is in exactly one cluster, so that $\sum n_k = N$, where $k = 1, \dots, K$. The mean vector M_k of cluster C_k is defined as the centroid of the cluster or

$$M_k = (1/n_k) \sum_{i=1}^{n_k} x_{ik} \quad (8)$$

Where x_{ik} is the i th sample belonging to cluster C_k . The square-error for cluster C_k is the sum of the squared Euclidean distances between each sample in C_k and its centroid. This error is also called the within - cluster variation:

$$e_k^2 = \sum_{i=1}^{n_k} (x_{ik} - M_k)^2 \quad (9)$$

The square - error for the entire clustering space containing K clusters is the sum of the within - cluster variations:

$$E_k^2 = \sum_{k=1}^K e_k^2 \quad (10)$$

The steps of K-means algorithm are shown as follows:

Step1: Select an initial partition with K clusters containing randomly chosen samples, and compute the centroids of the clusters.

Step2: Generate a new partition by assigning each sample to the closest cluster center.

Step3: Compute new cluster centers as the centroids of the clusters.

Step4: Repeat steps 2 and 3 until an optimum value of the criterion function is found (or until the cluster membership stabilizes) [10].

3.3 TOPSIS

The TOPSIS was first developed by Hwang & Yoon. According to this technique, the best alternative would be the one that is nearest to the positive-ideal solution and farthest from the negative ideal solution [11]. The calculation processes of the method are as following:

The first step is to convert the decision matrix $R = [r_{ij}]$ in a matrix of scale by using the following equation. If m is number of options and n is the number of criteria, and $N = [n_{ij}]_{m \times n}$ So, we have following equation:

$$n_{ij} = \frac{r_{ij}}{\sqrt{\sum_{i=1}^m (r_{ij})^2}} \quad (11)$$

Step 2: Calculate the weighted normalized decision matrix. The weighted normalized value v_{ij} is calculated as :

$$v_{ij} = w_j \times n_{ij} \quad , i=1, \dots, m, \quad j=1, \dots, n \quad (12)$$

Where w_j is the weight if the i th criterion, and $\sum_{j=1}^n w_j = 1$.

Step 3: Determine the positive ideal solutions and negative ideal solutions respectively

$$A^+ = \left\{ \left[\max_i V_{ij} \mid j \in J_1 \right], \left[\min_i V_{ij} \mid j \in J_2 \right] \mid i = 1, 2, \dots, m \right\} = \{V_1^+, \dots, V_m^+\} \quad (13)$$

$$A^- = \left\{ \left[\min_i V_{ij} \mid j \in J_1 \right], \left[\max_i V_{ij} \mid j \in J_2 \right] \mid i = 1, 2, \dots, m \right\} = \{V_1^-, \dots, V_m^-\} \quad (14)$$

Where J_1 is associated with the positive criteria, and J_2 is associated with the negative criteria

Step 4: Calculate the separation measures using the n -dimensional Euclidean distance. The separation of each alternative from the ideal solution is given as:

$$d_i^+ = \sqrt{\sum_{j=1}^n (v_{ij} - v_j^+)^2} \quad (15)$$

Similarly, the separation from the negative-ideal solution is given as

$$d_i^- = \sqrt{\sum_{j=1}^n (v_{ij} - v_j^-)^2} \quad (16)$$

Step 5: Calculate the relative closeness to the ideal solution. The relative closeness of the alternative A_i with respect to A^+ is defined as

$$CL = \frac{d_i^-}{d_i^- + d_i^+} \quad (17)$$

Step6: Rank the preference order. A large value of closeness coefficient indicates a good performance of the alternative A_i . The best alternative is the one with the greatest relative closeness to the ideal Solution [12].

4 Data

In this section, before the ranking the provinces, road safety measures have been identified. Based on data from the Road Maintenance & Transportation Organization (RMTO), 14 indicators of road safety were defined. This was so the indicators show the road safety of the provinces. Indicators are shown in Table 1.

Table 1 Indicators of road safety

Index	Definition
S1	Death rate of per 100,000 persons
S2	Injury rate of per 100,000 persons
S3	Death rate of per 100 kilometers
S4	Injury rate of per 100 kilometers
S5	Lighting rate of per 100 kilometers
S6	Speed Camera rate of per 100 kilometers
S7	Death rate to daily traffic volume
S8	Injury rate to daily traffic volume
S9	Emergency Base rate of 100,000 persons
S10	Crescent Base rate of 100,000 persons
S11	Emergency Base rate of 100 kilometers
S12	Crescent Base rate of 100 kilometers
S13	Average hours of training drivers
S14	The number of active police stations

5 Analysis of results

In this section, the results of the principal component analysis, cluster analysis and TOPSIS method were explored. In the presented research, the traffic accidents data of Iran's provinces is selected from 2013[13]. R software was used to conduct the principal component analysis and cluster analysis, then in order to execute the TOPSIS model; MATLAB 2012 Ra software was used.

5.1 Number of principal components to extract

Table 2 indicates that the first, second, third and forth principal components account for 42.6%, 17.5%, 10.4% and 8.8% of total variance respectively.

Table 2 Results of principal component analysis

	F1	F2	F3	F4	F5	F6	F7	F8	F9	F10	F11	F12	F13	F14
Standard Deviation	2.441	1.564	1.205	1.109	0.911	0.859	0.714	0.578	0.449	0.423	0.267	0.189	0.115	0.020
Proportion of Variance	0.426	0.175	0.104	0.088	0.059	0.053	0.036	0.024	0.014	0.013	0.005	0.003	0.001	0.000
Cumulative	0.426	0.600	0.704	0.792	0.851	0.904	0.940	0.964	0.979	0.991	0.996	0.999	1.000	1.000

In this paper, in order to determine the number of the principal components of the combination, a scree plot and parallel was used. The scree plot, proposed by Cattell, is very popular. In this rule, a plot of the eigenvalues against the number of components forms an "elbow". The number of principal components that need to be retained is shown by the elbow. In many instances, the scree plot may be so smooth that it may not be possible to determine a clear elbow. Hom has suggested a procedure, called parallel analysis. Figure 1 illustrates the two principal components that should be extracted. The first and second principal components account for 42.6% and 17.5% of the variance respectively. The cumulative distribution rate of the previous two principal components reached 60%.

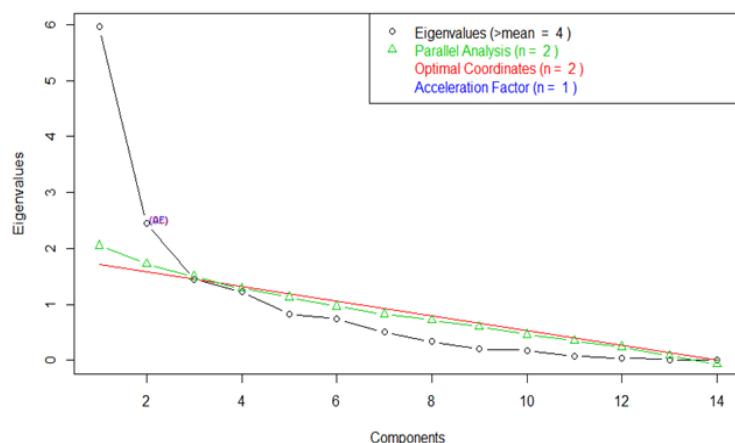


Fig.1 Scree plot and plot of eigenvalues from parallel analysis

5.2 Interpreting principal components

Since the principal components are linear combinations of the original variables, it is often necessary to interpret or provide a meaning for the linear combination. The higher the loading of a variable, the more influence it has in the formation of the principal component score and vice versa. Therefore, we can use the loadings to determine which variables are influential in the formation of the principal components, and we can then assign a meaning or label to the principal component. In this paper, the loading value of .65 has been used as the cutoff point. As shown in Table 3, loading values which are more than .65 were highlighted. It can be said that the first principal component (PC1) represents the road index, and the second principal component represents the monitoring and control index. In other words, the first principal component is a measure of the index of death rate of per 100 kilometers, injury rate of per 100 kilometers, lighting rate of per 100 kilometers, speed cameras rate per 100 kilometers, emergency bases rate of per 100 kilometers and crescent bases rate of per 100 kilometers across the provinces. The second principal component (PC2) is a measure of the index of injury rate to daily traffic volume and the number of active police bases. Therefore, PC1 can be labeled as the road index and PC2 as the monitoring and control index. The principal components' scores are shown in Table 4.

Table 3 Loading values

	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13	S14
PCA1	0.52	0.09	-0.92	-0.90	-0.92	-0.76	0.55	0.54	0.61	0.48	-0.88	-0.76	0.17	0.145
PCA2	0.42	0.38	-0.17	-0.19	0.10	0.20	-0.53	-0.67	0.52	0.63	-0.02	0.22	-0.22	-0.73

Table 4 Principal components scores

Province	PCA1	PCA2	Province	PCA1	PCA2
Sharghi	0.119699	-1.51199	Qazvin	-0.781	1.513431
Gharbi	0.45007	-1.34437	Qom	-3.44641	1.79814
Ardebil	-0.24543	0.348708	Kordestan	0.741826	-0.46933
Esfahan	0.620427	-1.72697	Kerman	1.794277	-1.40594
Alborz	-7.50009	0.590583	Kermanshah	0.955223	-0.93271
Eilam	1.547405	2.464702	Kohkiloye	1.448702	0.445264
Boshehr	0.809103	0.894224	Golestan	-1.12893	0.435193
Tehran	-7.76818	-2.01037	Gilan	-0.77332	-0.30495
Charmahal	0.722998	0.913938	Lorestan	-0.03438	-0.39358
Khorasan joonobi	3.811955	2.540165	Mazandaran	-1.42206	0.085742
Khorasan razvi	1.149812	-2.87296	Markazi	0.343605	0.72947
Khorasan shomali	-0.1953	1.65435			
Khozestan	1.061681	-2.20977	Hormozgan	0.293537	0.462625
Zanjan	0.299977	1.051823			
Cemnan	1.721491	2.676066	Hamedan	-0.15355	0.396849
Sistan va Balochestan	3.497397	-3.26291			
Fars	1.276283	-1.40849	Yazd	0.783183	0.853083

5.3 Index of Road Traffic Safety (IRTS)

The scores of the principal components (road and monitoring and control) are used to create the index of road traffic safety that is shown in Table 5. Based on the safety index, the provinces can be ranked. The greater the IRTS, the worse the road traffic safety condition will be.

Table 5 Result of provinces ranking

Province	Rank	IRTS	Province	Rank	IRTS	Province	Rank	IRTS
Tehran	1	-3.6573	Esfahan	12	-0.0376	Charmahal	23	0.4674
Alborz	2	-3.0889	Khorasan razvi	13	-0.0125	Yazd	24	0.4824
Qom	3	-1.1527	Hamedan	14	0.0040	Boshehr	25	0.5006
Mazandaran	4	-0.5902	Khozestan	15	0.0658	Kerman	26	0.5180
Golestan	5	-0.4044	Hormozgan	16	0.2057	Kohkiloye	27	0.6944
Gilan	6	-0.3824	Khorasan	17	0.2059	Sistan va	28	0.9185
Azarbayan	7	-0.2132	Kordestan	18	0.2337	Balochestan	29	1.0892
Lorestan	8	-0.0834	Kermanshah	19	0.2436	Eilam	30	1.2002
Qazvin	9	-0.0680	Markazi	20	0.2737	Cemnan	31	2.0661
Ardebil	10	-0.0435	Fars	21	0.2971	Khorasan Joonobi	32	
Azarbayan	11	-0.0433	Zanjan	22	0.3114			

5.4 Clustering provinces in terms of safety

In this section, the principal components' scores (road and monitoring and control) were used to cluster the provinces with the use of the K-means method. For this purpose, the number of clusters must first be determined. The number of clusters is determined based on within groups sum of square. For this purpose, Figure 2 plots of the sum of the squares within the cluster against the number of components and is examined for an "elbow". According to Figure 2, when the number of clusters were increasing, the sum of the squares within the cluster were decreasing. Figure 2 shows the optimal number of clusters as 4. Four clusters are shown in table 6.

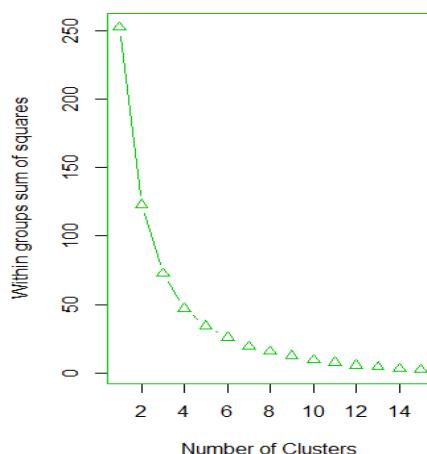


Fig. 2 Number of cluster vs within groups sum of squares

Table 6 Provinces clustering

Cluster	Province
1	Tehran- Alborz
2	Eilam- Cemnan- Khorasan Joonobi
3	Azarbayan Sharghi- Azarbayan Gharbi- Esfahan- Khorasan Razvi- Khozestan- Kordestan- Kermanshah- Fars- Kerman- Sistan va Baluchestan
4	Qom- Mazandaran- Golestan- Gilan- Lorestan- Qazvin- Ardebil- hamedan- Hormozgan- Khorasan Shomali- Markazi- Zanjan- Charmahal- Yazd- Boshehr- Kohkiloye

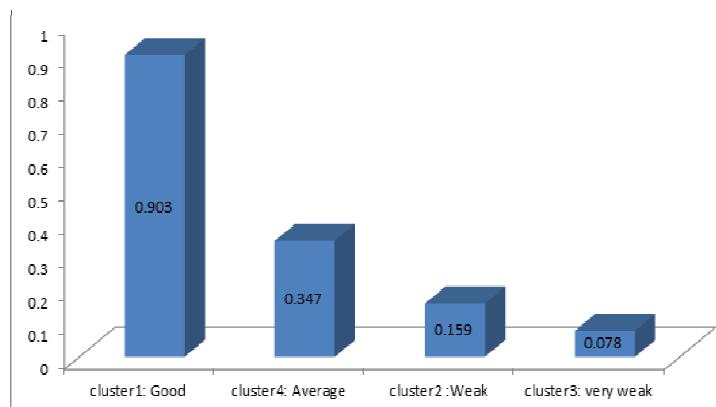
K-means clustering was applied to the safety level classifications of the provinces. In accordance with the K-means clustering method, road traffic safety was divided into four levels. In this paper, to examine the status of each cluster in terms of safety levels, average values for each index in different clusters were calculated. These can be seen in table 7. The weight of each index was then extracted based on a Shannon Entropy method. Statistics in relation to weight are provided in table 8. The status of safety levels was determined using a TOPSIS model and the results of model are shown in Figure 3.

Table 7 Average values for each index in different clusters

	s1	s2	s3	s4	s5	s6	s7	s8	s9	s10	s11	s12	s13	s14
Cluster1	13.52	314.39	110.13	2627.13	24.52	3.33	0.01	0.21	0.68	0.16	5.09	1.20	3.57	7.00
Cluster2	39.10	518.86	11.38	156.91	3.04	0.00	0.05	0.62	5.30	2.12	1.50	0.59	3.69	6.00
Cluster3	25.80	413.57	19.77	339.85	3.06	0.20	0.07	0.97	1.87	0.52	1.40	0.40	4.66	10.60
Cluster4	27.66	470.36	22.52	396.39	7.20	0.90	0.02	0.43	2.20	0.85	1.59	0.60	4.58	5.76

Table 8 Weights of each index in Shannon Entropy

w1	0.10%	w8	12.84%
w2	0.34%	w9	0.53%
w3	0.35%	w10	4.71%
w4	0.49%	w11	0.34%
w5	13.95%	w12	3.17%
w6	36.85%	w13	0.01%
w7	18.97%	w14	7.35%

**Fig. 3** Result of clusters ranking in TOPSIS method

As can be seen in Figure 3, the first cluster, which includes the Tehran and Alborz provinces, has the highest TOPSIS value of 0.9. These can therefore be labeled as having a good level in terms of safety. The fourth cluster, which includes the Qom, Mazandaran, Golestan, Gilan, Lorestan, Qazvin, Ardebil, Hamedan, Hormozgan, Khorasan Shomali, Markazi, Zanjan, Charmahal, Yazd, Boshehr and Kohkiloye provinces has the second highest TOPSIS value of 0.35. The fourth cluster is much different from the first cluster and is labeled as having an average level of safety. The second cluster, which includes the Eilam, Cemnan and Khorasan Joonobi provinces, has TOPSIS value 0.16 – the third highest. This is therefore labeled as having a weak level of safety. As a result, there are four levels that can be used as labels: good, average, poor and very poor. Results of the methods are provided in Table 9. We can infer that the results of the hybrid combination of K-means classification and TOPSIS with ranking in terms of IRTS are similar to one another.

6 Conclusion

In the present study, an index system was defined which consists of 14 relative indexes for road traffic safety evaluation. Using a PCA method to reduced the dimensions of the multi-index data to 2 components. The Index of Road Traffic Safety (IRTS) was constructed for the ranking of the road traffic safety situation. In the second section, the K-means clustering method was applied in order to classify provinces by taking 2 principal components and splitting them into 4 clusters. Then, through the use of a TOPSIS technique, the status of each cluster was examined in terms of safety levels. Results of the hybrid combination of model k-means classification and TOPSIS with ranking by IRTS are similar to one another. In this way, the first cluster, which included the Tehran and Alborz provinces, has a good status in

safety. The fourth cluster, which included the Qom, Mazandaran, Golestan, Gilan, Lorestan, Qazvin, Ardebil, Hamedan, Hormozgan, Khorasan Shomali, Markazi, Zanjan, Charmahal, Yazd, Boshehr and Kohkiloye provinces has an average status in safety due to the fact that the TOPSIS value is less than the TOPSIS value of the first cluster. The second cluster, which included the Eilam, Cemnan and Khorasan Joonobi provinces, was weak in safety. Finally, the third cluster, which included the Azarbayjan Sharghi, Azarbayjan Gharbi, Esfahan, Khorasan Razvi, Khozestan, Kordestan, Kermanshah, Fars, Kerman and Sistan va Baluchestan provinces was very weak. This article provides good information for transportation planners to recognize the critical provinces in terms of 14 relative indexes to enable the efficient allocation of limited resources.

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